

A GENERAL FOURTH-ORDER PARABOLIC EQUATION

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Abstract. In this paper we establish the existence and uniqueness of weak solutions for the initial-boundary value problem of a general fourth-order parabolic equation. Our assumptions are much weaker than those in the literature.

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