

ON THE HYDROSTATIC STOKES APPROXIMATION WITH NON HOMOGENEOUS DIRICHLET BOUNDARY CONDITIONS

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Abstract. We deal with the hydrostatic Stokes approximation with non homogeneous Dirichlet boundary conditions. After having investigated the homogeneous case, we build a lifting operator of boundary values related to the divergence operator, and solve the non homogeneous problem in a cylindrical type domain.

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