

## ON A CLASS OF ABSTRACT FUNCTIONAL DIFFERENTIAL EQUATIONS INVOLVING ALMOST SECTORIAL OPERATORS

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*Abstract.* We study the existence of mild solutions for a class of abstract functional differential equations involving almost sectorial operators. A concrete application to delayed partial differential equations is presented.

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