

EXISTENCE AND UNIQUENESS OF A POSITIVE SOLUTION TO GENERALIZED NONLOCAL THERMISTOR PROBLEMS WITH FRACTIONAL-ORDER DERIVATIVES

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Abstract. In this work we study a generalized nonlocal thermistor problem with fractional-order Riemann–Liouville derivative. Making use of fixed-point theory, we obtain existence and uniqueness of a positive solution.

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