

## EXISTENCE OF MILD SOLUTION FOR IMPULSIVE STOCHASTIC DIFFERENTIAL EQUATIONS WITH NONLOCAL CONDITIONS

LIJUN PAN

*Abstract.* This paper is concerned with the existence of mild solution for impulsive stochastic differential equations with nonlocal conditions in  $PC$ -norm. Our approach is based on Krasnoselskii fixed point theorem.

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