

EXISTENCE OF POSITIVE SOLUTIONS FOR A FOURTH ORDER DIFFERENTIAL INCLUSION

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Abstract. We prove an existence result for positive solutions of a fourth order differential inclusion. The proof is accomplished through the use of Green's functions and a fixed point theorem. One of the technical assumptions is explored in detail.

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