

COMPOSITION CONDITIONS FOR TWO-DIMENSIONAL POLYNOMIAL SYSTEMS

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Abstract. Several papers published recently about the center composition condition of Abel differential equations and two-dimensional polynomial systems with homogeneous nonlinearities. We give necessary and sufficient conditions for the existence of composition centers for general two-dimensional polynomial systems.

Mathematics subject classification (2010): 34C07, 34C05, 34C25, 37G15.

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