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INFINITELY MANY SOLUTIONS FOR KIRCHHOFF TYPE PROBLEMS

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Abstract. This paper is devoted to the study of infinitely many solutions for a class of Kirchhoff type problems on a bounded domain. Based on the Fountain Theorem of Bartsch, we obtain the multiplicity results, which unify and sharply improve the recent results of He and Zou [X. He, W. Zou, Multiplicity of solutions for a class of Kirchhoff type problems, Acta Math. Appl. Sin. (Engl. Ser.) 26 (2010) 387-394].

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