

ASYMPTOTICS FOR NONLOCAL EVOLUTION PROBLEMS BY SCALING ARGUMENTS

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Abstract. In this paper we consider a nonlocal evolution problem and obtain by a scaling method the first term in the asymptotic behavior of the solutions. The method employed treats in different way the smooth and the rough part of the solution.

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