

POSITIVE SOLUTIONS FOR SINGULAR NONLOCAL BOUNDARY VALUE PROBLEMS INVOLVING NONLINEAR INTEGRAL CONDITIONS

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Abstract. In this paper, using the fixed point theory on a cone and Leray-Schauder fixed point theorem, we present some existence results for singular nonlocal boundary value problems involving nonlinear integral conditions. Our nonlinearity may be singular in its dependent variable and it is allowed to change sign.

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