

EXISTENCE AND GLOBAL ATTRACTIVITY OF PERIODIC SOLUTIONS FOR CHEMOSTAT MODEL WITH DELAYED NUTRIENTS RECYCLING

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Abstract. In this paper, a chemostat model involving distributed delays with two-microorganism and nutrients recycling is considered. Some sufficient conditions ensuring the existence and global attractivity of periodic solutions for the chemostat model are derived by employing the theory of coincidence degree and differential inequality technique.

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