

OSCILLATION CRITERIA FOR HALF-LINEAR DIFFERENTIAL EQUATIONS WITH $p(t)$ -LAPLACIAN

YUTAKA SHOUKAKU

Abstract. This paper presents sufficient conditions for oscillation of solutions of half-linear differential equations with $p(t)$ -Laplacian. As an application of generalized Riccati-type inequality, some new oscillation theorems are established.

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