

EXISTENCE OF A NON-TRIVIAL SOLUTION FOR NONLINEAR DIFFERENCE EQUATIONS

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Abstract. The existence of a non-trivial solution for a discrete non-linear Dirichlet problem involving p -Laplacian is investigated. The technical approach is based on a local minimum theorem for differentiable functionals due to Bonanno.

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