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EXISTENCE RESULTS FOR A NONLINEAR FRACTIONAL DIFFERENTIAL EQUATIONS WITH INTEGRAL BOUNDARY CONDITIONS ON THE HALF–LINE

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Abstract. By means of nonlinear alternative theorem of Leray-Schauder, some new results on the existence of positive solutions for a nonlinear fractional differential equations with integral boundary conditions on unbounded domain are established. The paper concludes with an illustrative example.

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