

ON THE SOLUTIONS OF SOME SEMILINEAR INTEGRO-DIFFERENTIAL INCLUSIONS

AURELIAN CERNEA

Abstract. We consider Cauchy problems associated to first and second order semilinear integro-differential inclusions in separable Banach spaces and we establish some Filippov type existence results.

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