

## POSITIVE SOLUTIONS FOR A FOURTH ORDER DIFFERENTIAL INCLUSION WITH BOUNDARY VALUES

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*Abstract.* An existence result for positive solutions of a fourth order differential inclusion is proven. This is accomplished by using a certain fixed point theorem on cones and a minor extension of the Ascoli theorem. This inclusion allows both the function and its derivative on the right-hand side.

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