

EXISTENCE OF SOLUTIONS FOR AN ELLIPTIC BOUNDARY VALUE PROBLEM VIA A GLOBAL MINIMIZATION THEOREM ON HILBERT SPACES

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Abstract. We present a new global minimization theorem on Hilbert spaces which is different from the one in Hofer [7] using the notion of a nonexpansive potential operator. An example is given to illustrate our result.

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