

## ON THE OSCILLATION CERTAIN FOURTH ORDER NONLINEAR DYNAMIC EQUATIONS WITH A NONLINEAR MIDDLE TERM

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*Abstract.* New oscillation criteria for certain fourth order nonlinear dynamic equations with nonlinear middle term are established.

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