

CONTINUOUS DEPENDENCE FOR SOLUTIONS TO 2–D BOUSSINESQ SYSTEM CHANNEL FLOW

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Abstract. This paper considers the 2-D Boussinesq system in a semi-infinite channel. By making use of the earlier work of [19] and some Soblev inequalities, the continuous dependence on the coefficient of the system is obtained. The authors also show how to bound the total energy.

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