

EXISTENCE AND MULTIPLICITY OF SOLUTIONS FOR KIRCHHOFF TYPE PROBLEMS WITH PARAMETER

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Abstract. In this paper, we study Kirchhoff type problems with parameter on a bounded domain. By using variational methods, we prove the existence and multiplicity of weak solutions.

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