

## ON A GENERALIZATION OF THE LIOUVILLE FORMULA

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*Abstract.* In this article, we obtain a new formula which generalizes the Liouville formula of the linear differential system to nonlinear differential system. We establish the relationship between the Jacobi determinant of the first integral and the trace of Jacobi matrix of the  $n$ -dimensional vector field.

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