

POSITIVE SOLUTIONS FOR A CLASS OF FRACTIONAL DIFFERENCE BOUNDARY VALUE PROBLEMS

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Abstract. In this paper using the fixed point index and the Leggett-Williams fixed point theorem we establish the existence and multiplicity of positive solutions for a class of fractional difference boundary value problems.

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