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POSITIVE SOLUTIONS FOR FRACTIONAL INTEGRO–BOUNDARY VALUE PROBLEM OF ORDER $(1,2)$ ON AN UNBOUNDED DOMAIN

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Abstract. In this manuscript, we study a system of fractional integro boundary value problem on unbounded domain. The solution of the system is defined in terms of the Green's function. We have established the existence and uniqueness results by utilizing the fixed point theorems. The main outcomes and assumptions are verified via some examples.

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