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OSCILLATORY BEHAVIOR OF SECOND ORDER NONLINEAR DELAY DIFFERENTIAL EQUATIONS WITH POSITIVE AND NEGATIVE NEUTRAL TERMS

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Abstract. The aim of the paper is to initiate a study of the oscillation of solutions of second order nonlinear differential equations with positive and negative nonlinear neutral terms. The results are illustrated by some examples.

Mathematics subject classification (2010): 34C10, 34K11.
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