

EXISTENCE OF SOLUTION FOR NON-AUTONOMOUS SEMILINEAR MEASURE DRIVEN EQUATIONS

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Abstract. This work is concerned with the existence of a solution for non-autonomous measure driven semilinear equation in Banach spaces. The Schauder fixed point theorem is utilized to explore the existence of a solution. Finally, we construct an example to demonstrate the acquired outcomes.

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