

EXISTENCE OF THREE POSITIVE SOLUTIONS FOR BOUNDARY VALUE PROBLEMS OF SINGULAR FRACTIONAL DIFFERENTIAL EQUATIONS

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Abstract. In this article, we establish the existence of at least three unbounded positive solutions to a boundary-value problem of the nonlinear singular fractional differential equation. Our analysis rely on the well known fixed point theorem in a cone.

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