

THE SOLUTION OF FRACTIONAL NONLINEAR GINZBURG–LANDAU EQUATION WITH WEAK INITIAL DATA

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Abstract. In this paper, we study the solution of the fractional nonlinear Ginzburg-Landau (FNGL) equation with weak initial data in the weighted Lebesgue spaces. The existence of a solution to this equation is proved by the contraction-mapping principle.

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