SOME DISCRETE FRACTIONAL LYAPUNOV–TYPE INEQUALITIES

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Abstract. In this work we obtain Lyapunov-type inequalities for two-point conjugate and right-focal boundary value problems depending on discrete fractional operators Δ^{α}, $1 < \alpha \leqslant 2$.

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