

POSITIVE SOLUTIONS TO ITERATIVE SYSTEMS OF FRACTIONAL ORDER THREE-POINT BOUNDARY VALUE PROBLEMS WITH RIEMANN-LIOUVILLE DERIVATIVE

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Abstract. In this paper, we determine the eigenvalues λ_i , $1 \leq i \leq n$, for which there exist positive solutions for the iterative system of fractional order three-point boundary value problems by applying fixed point theorem.

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