

ON THE CAUCHY PROBLEM OF A DELAY STOCHASTIC DIFFERENTIAL EQUATION OF ARBITRARY (FRACTIONAL) ORDERS

A. M. A. EL-SAYED, E. E. ELADDAD AND H. F. A. MADKOUR

Abstract. In this work, we are concerned with the Cauchy problem of a delay stochastic differential equation of arbitrary (fractional) orders. The existence (local) of a unique mean square continuous solution is proved. The continuous dependence of the solution on the initial random variable is studied.

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