GLOBAL EXISTENCE AND UNIQUENESS FOR IMPLICIT DIFFERENTIAL EQUATION OF ARBITRARY ORDER

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Abstract. The aim of this paper is to establish the existence result for implicit differential equation of fractional (arbitrary) order via topological transversality theorem known as Leray-Schauder alternative. Further we prove the uniqueness results. The Grownwall's lemma for singular kernels play an important role to prove our results. We verify our results by providing an example.

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