

Chebyshev Type Inequality on Nabla Discrete Fractional Calculus

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Abstract. In this paper, we establish some Chebyshev type inequalities on discrete fractional calculus with nabla operator (or backward difference operator).

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