

CONTINUOUS DEPENDENCE OF THE SOLUTION OF RANDOM FRACTIONAL-ORDER DIFFERENTIAL EQUATION WITH NONLOCAL CONDITIONS

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Abstract. In this paper we are concerned with an initial value problem of random fractional-order differential equation with nonlocal condition. Continuous dependence and some other properties concerning the existence and uniqueness of the solution will be proved.

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