INEQUALITIES OF THE HERMITE–HADAMARD
TYPE FOR QUASI–CONVEX FUNCTIONS VIA THE
(k,s)–RIEMANN–LIOUVILLE FRACTIONAL INTEGRALS

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Abstract. Recently, Hussain et al. in the paper [Some k-fractional associates of Hermite–Hadamard's inequality for quasi-convex functions and applications to special means, Fractional Differential Calculus, **7**(2) 2017, 301–309] established some new Hermite–Hadamard type inequalities for functions whose absolute values are quasi-convex via the k-Riemann–Liouville fractional integral operators. The purpose of this article is to extend and generalize the results, obtained in the aforementioned paper, via the (k,s)-fractional integrals.

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