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ON ASYMPTOTIC PROPERTIES OF SOME NEUTRAL DIFFERENTIAL EQUATIONS INVOLVING RIEMANN–LIOUVILLE FRACTIONAL DERIVATIVE

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Abstract. The main purpose of the present note is to investigate asymptotic properties of some neutral delay differential equations involving Reimann-Liouville fractional derivative by means of Lyapunov functions. Integer order derivatives are used to overcome the difficulties of calculating the derivatives of Lyapunov functions. Two examples are given to illustrate the results.

Mathematics subject classification (2020): 34K20, 34K40.
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