

## EXISTENCE AND UNIQUENESS RESULTS FOR GENERALIZED CAPUTO ITERATIVE FRACTIONAL BOUNDARY VALUE PROBLEMS

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*Abstract.* In this paper, we present some results on existence and uniqueness for a class of boundary value problems for iterative fractional differential equations with generalized Caputo fractional derivative. For our proofs, we employ some suitable fixed point theorems. Finally, we provide an illustration for more clarity.

*Mathematics subject classification (2020):* 26A33, 34K10, 34A08, 34K37.

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