

ABSTRACT FRACTIONAL DIFFERENTIAL EQUATIONS WITH CAPUTO–FABRIZIO DERIVATIVE

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Abstract. The main objective of this paper is to prove the existence and uniqueness of mild solution for abstract differential equations by using the resolvent operators and fixed point theorem. Moreover, we studied some examples on partial differential equation with Caputo-Fabrizio derivative.

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