

SUFFICIENT CONDITIONS FOR STARLIKENESS

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Abstract. The purpose of the present paper is to consider some sufficient conditions for analytic functions in the open unit disk to be starlike. Here we establish three theorems by using Jack's lemma and a simple result contained in Lemma 2.2. Our theorems provide improvements of the results about sufficient conditions for starlike functions given earlier by Lewandowski et al. [2], Li and Owa [3], Nunokawa et al. [5] and Ramesha et al. [6].

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