

ON p -ADIC INTERPOLATING FUNCTION ASSOCIATED WITH MODIFIED DIRICHLET'S TYPE OF TWISTED q -EULER NUMBERS AND POLYNOMIALS WITH WEIGHT α

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Abstract. In the present paper, we introduce modified Dirichlet's type of twisted q -Euler polynomials with weight α . We apply the method of generating function and p -adic q -integral representation on \mathbb{Z}_p , which are exploited to derive further classes of q -Euler numbers and polynomials. Our new generating function possess a number of interesting properties which we state in this paper.

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