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CERTAIN SUBORDINATION RESULTS INVOLVING A GENERALIZED MULTIPLIER TRANSFORMATION OPERATOR

POONAM SHARMA, J. K. PRAJAPAT AND R. K. RAINA

Abstract. This paper investigates various new subordination results for certain p-valent analytic functions involving a generalized multiplier transformation operator $J_p^m(\lambda,l), m \in \mathbb{Z}$, defined recently by J. K. Prajapat [Math. Comput. Modelling, 55 (2012), 1456–1465]. Several lines of approach are followed to obtain the subordination results. We also consider some simpler and precise forms of the derived results.

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