

SOME INEQUALITIES FOR THE GENERALIZED SINE AND THE GENERALIZED HYPERBOLIC SINE

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Abstract. In this paper, the authors establish some new inequalities for the generalized sine and the generalized hyperbolic sine.

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