

SOME PROPERTIES AND INEQUALITIES FOR h -GEOMETRICALLY CONVEX FUNCTIONS

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Abstract. In the paper, the definition of h -geometrically convex functions is introduced, some properties of h -geometrically convex functions are studied, and several integral inequality for the newly defined functions are established.

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