

A MIXED PARSEVAL–PLANCHEREL FORMULA

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Abstract. In this note, a general formula is proved. It expresses the integral on the line of the product of a function f and a periodic function g in terms of the Fourier transform of f and the Fourier coefficients of g . This allows the evaluation of some oscillatory integrals.

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