

SOME STABILITY RESULTS RELATED TO SOME FIXED POINT THEOREMS

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Abstract. In this paper, we introduce two types of stability and we investigate some fixed point theorems, as Schauder Theorem, Borsuk Theorem and Knaster Lemma, from this viewpoint.

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