

PARTIAL SUMS OF NORMALIZED DINI FUNCTIONS

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Abstract. Some lower bounds are proposed for the quotients of normalized Dini functions and their partial sum, as well as for the quotients of the derivative of normalized Dini functions and their partial sums. Our study is motivated by some earlier results one similar lower bounds for quotients of convex univalent functions and their partial sum.

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