

## ON STATISTICAL CONVERGENCE WITH RESPECT TO MEASURE

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*Abstract.* Several notions of convergence for subsets of metric spaces appear in the literature. In this paper, for real valued measurable functions defined on a measurable space  $(X, \mathcal{M}, \mu)$ , we obtain a statistical version of Lebesgue's bounded convergence theorem (when  $\mu(X) < \infty$ ) and examine the validity of the classical theorems of Measure Theory for statistical convergences.

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