

## INITIAL BOUNDS FOR ANALYTIC AND BI-UNIVALENT FUNCTIONS BY MEANS OF CHEBYSHEV POLYNOMIALS

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*Abstract.* In this paper, we obtain initial coefficient bounds for functions belong to a subclass of bi-univalent functions by using the Chebyshev polynomials and also we find Fekete-Szegő inequalities for this class.

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