

## ON AN EXTENSION OF EXTENDED BETA AND HYPERGEOMETRIC FUNCTIONS

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*Abstract.* Motivated mainly by certain interesting recent extensions of the Gamma, Beta and hypergeometric functions, we introduce here new extensions of the Beta function, hypergeometric and confluent hypergeometric functions. We systematically investigate several properties of each of these extended functions, such as their various integral representations, Mellin transforms, derivatives, transformations, summation formulas, generating function and asymptotics. Relevant connections of certain special cases of the main results presented herewith are also pointed out.

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