

## BOUNDARY SCHWARZ INEQUALITIES ARISING FROM ROGOSINSKI'S LEMMA

PETER R. MERCER

*Abstract.* We consider some Schwarz and Carathéodory inequalities at the boundary, as consequences of a lemma due to Rogosinski.

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