

ON A SUBCLASS OF ANALYTIC CLOSE-TO-CONVEX FUNCTIONS IN q -ANALOGUE ASSOCIATED WITH JANOWSKI FUNCTIONS

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Abstract. In this article we define a new subclass of analytic multivalent close-to-convex functions in q -calculus associated with Janowski functions. We investigate some geometric properties such as sufficiency criteria, distortion problem, growth theorem, radii of starlikeness and convexity and coefficient estimates for this class.

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